

# Model-based Analysis and Processing of Speech and Audio Signals

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Mads Græsbøll Christensen

Audio Analysis Lab, CREATE  
Aalborg University, Denmark



**AALBORG UNIVERSITY**  
DENMARK



# Preface

- ▶ Looking back, there are certain ideas that permeate my research over the past decades.
- ▶ Briefly put, my research has revolved around the ideas of
  - ▶ describing and analyzing audio signals using parametric and statistical models.
  - ▶ posing, analyzing, and solving problems in speech and audio using optimization, linear algebra, and statistics.
- ▶ In this presentation, I would like to talk more about the *model-based approach* and what can be achieved with it.
- ▶ I will do this primarily in the context of a specific model and our contributions.



# Outline

Model-based Approach

Harmonic Model

Fundamental Frequency Estimation

Pre-whitening

Separation & Noise Reduction

Non-Stationarity

Array Processing

Contributions & Conclusions

# Model-based Approach



**Research questions:** *What are good models of speech and audio signals recorded in adverse conditions, how do we find their parameters, and how can we use them?*



# Model-based Approach

- ▶ Processing based on generative signal models described in terms of physically meaningful parameters.
- ▶ Speech and audio models have been around for many years (*we tried it in the 70s and it didn't work*).
- ▶ Skeptics argue that the models are (always) wrong and that it is not possible to estimate the parameters anyway.
- ▶ However, models can be used for many things and in different ways.
- ▶ The approach leads to robust, tractable and often fast methods that can be improved and analyzed.



# Model-based Approach

*Partial models, imperfect as they may be, are the only means developed by science for understanding the universe.*

*Rosenblueth & Wiener, 1945.*



# Model-based Approach

What is a good model?

- ▶ Fits the data well
- ▶ Physically meaningful
- ▶ As simple as possible!

We will now explore with an example how we can

- ▶ model speech and audio signals
- ▶ estimate parameters
- ▶ use and improve the model

# Harmonic Model

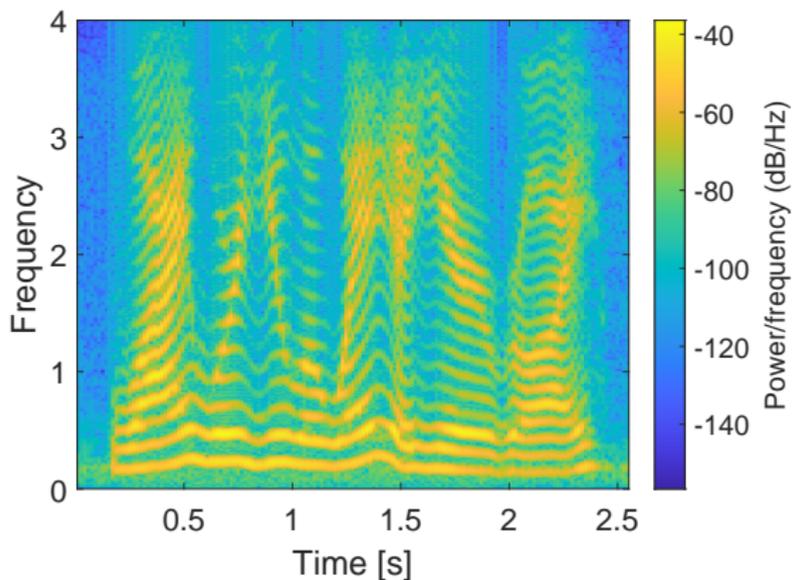


Figure: Spectrogram of speech utterance "why were you away a year, Roy?".



# Harmonic Model

Many speech and audio signals are periodic or approximately so. Such signals can be modeled by the harmonic model given by (for  $n = 0, \dots, N - 1$ )

$$x(n) = s(n) + e(n) \quad (1)$$

$$= \sum_{l=1}^L a_l e^{j\omega_0 l n} + e(n). \quad (2)$$

Definitions:

$s(n)$  is the deterministic component

$e(n)$  is the stochastic/noise component

$\omega_0$  is the fundamental frequency

$a_l = A_l e^{j\phi_l}$  is the complex amplitude of the  $l$ th harmonic

$\theta = [\omega_0 \ A_1 \ \phi_1 \ \dots \ A_L \ \phi_L]^T$  is the parameter vector



# Harmonic Model

The model can be written in matrix-vector notation as

$$\mathbf{x}(n) = \mathbf{s}(n) + \mathbf{e}(n) \quad (3)$$

$$= \mathbf{Z}(n)\mathbf{a} + \mathbf{e}(n) \quad (4)$$

$$= \mathbf{ZD}(n)\mathbf{a} + \mathbf{e}(n) \quad (5)$$

with the following definitions:

$$\mathbf{x}(n) = [ x(n) \cdots x(n+M-1) ]^T$$

$$\mathbf{z}(n, \omega) = [ e^{j\omega n} e^{j\omega(n+1)} \cdots e^{j\omega(n+M-1)} ]^T$$

$$\mathbf{Z}(n) = [ \mathbf{z}(n, \omega_0) \cdots \mathbf{z}(n, \omega_0 L) ], \mathbf{Z} = \mathbf{Z}(0)$$

$$\mathbf{D}(n) = \text{diag}([ e^{j\omega_0 n} e^{j\omega_0 2n} \cdots e^{j\omega_0 Ln} ])$$

$$\mathbf{a} = [ a_1 \cdots a_L ]^T$$



# Harmonic Model

The covariance matrix of  $\mathbf{x}(n)$  denoted  $\mathbf{R} = \mathbb{E} \{ \mathbf{x}(n) \mathbf{x}^H(n) \}$ , can be written in terms of the model, i.e.,

$$\mathbf{R} = \mathbf{Z} \mathbf{P} \mathbf{Z}^H + \mathbf{Q}, \quad (6)$$

where  $\mathbf{P} \approx \text{diag} ([ A_1^2 \ \dots \ A_L^2 ])$  and  $\mathbf{Q} = \mathbb{E} \{ \mathbf{e}(n) \mathbf{e}^H(n) \}$ . Often it is assumed that  $\mathbf{Q} = \sigma^2 \mathbf{I}$ .

Let the output signal  $y(n)$  of a filter having coefficients  $\mathbf{h} \in \mathbb{C}^M$  be defined as

$$y(n) = \mathbf{h}^H \mathbf{x}(n) \quad (7)$$

$$= \mathbf{h}^H \mathbf{Z} \mathbf{D}(n) \mathbf{a} + \mathbf{h}^H \mathbf{e}. \quad (8)$$

The output power  $\mathbf{h}^H \mathbf{R} \mathbf{h}$  is then

$$\mathbb{E} \{ |y(n)|^2 \} = \mathbf{h}^H \mathbf{Z} \mathbf{P} \mathbf{Z}^H \mathbf{h} + \mathbf{h}^H \mathbf{Q} \mathbf{h}. \quad (9)$$



# Harmonic Model

Let the EVD of  $\mathbf{R}$  be

$$\mathbf{R} = \mathbf{U}\mathbf{\Lambda}\mathbf{U}^H, \quad (10)$$

where  $\mathbf{U}$  contains the  $M$  eigenvectors  $\mathbf{u}_k$  of  $\mathbf{R}$ , i.e., and  $\mathbf{\Lambda}$  is a diagonal matrix containing the corresponding (sorted) eigenvalues,  $\lambda_k$ .

Let  $\mathbf{S}$  and  $\mathbf{G}$  be formed as

$$\mathbf{S} = [ \mathbf{u}_1 \quad \cdots \quad \mathbf{u}_L ] \quad \text{and} \quad \mathbf{G} = [ \mathbf{u}_{L+1} \quad \cdots \quad \mathbf{u}_M ]. \quad (11)$$

Assuming  $\mathbf{Q} = \sigma^2\mathbf{I}$  and observing that  $\mathbf{U}(\mathbf{\Lambda} - \sigma^2\mathbf{I})\mathbf{U}^H = \mathbf{ZPZ}^H$  it follows that

$$\mathbf{Z}^H\mathbf{G} = \mathbf{0} \quad \text{and} \quad \mathcal{R}(\mathbf{S}) = \mathcal{R}(\mathbf{Z}). \quad (12)$$



# Harmonic Model

Is it possible to

- ▶ estimate the nonlinear parameters?
- ▶ take non-stationarity into account?
- ▶ deal with interference and noise?
- ▶ extend the model to arrays?

Let us find out...



# Fundamental Frequency Estimation

The variance of an unbiased estimate  $\hat{\theta}_i$  of  $\theta_i$  (i.e., the  $i$ th element of  $\boldsymbol{\theta} \in \mathbb{R}^P$ ) is bounded by the Cramér-Rao lower bound (CRLB):

$$\text{var}(\hat{\theta}_i) \geq [\mathbf{I}^{-1}(\boldsymbol{\theta})]_{ii}, \quad (13)$$

where the Fisher Information Matrix (FIM)  $\mathbf{I}(\boldsymbol{\theta})$  is given by

$$[\mathbf{I}(\boldsymbol{\theta})]_{ii} = -\text{E} \left\{ \frac{\partial^2 \ln p(\mathbf{x}; \boldsymbol{\theta})}{\partial \theta_i \partial \theta_i} \right\}, \quad (14)$$

with  $\ln p(\mathbf{x}; \boldsymbol{\theta})$  being the log-likelihood function for  $\mathbf{x} \in \mathbb{C}^N$ . The asymptotic CRLB for  $\omega_0$  (for WGN) is

$$\text{var}(\hat{\omega}_0) \geq \frac{6\sigma^2}{N^3 \sum_{l=1}^L A_l^2 l^2}. \quad (15)$$



# Fundamental Frequency Estimation

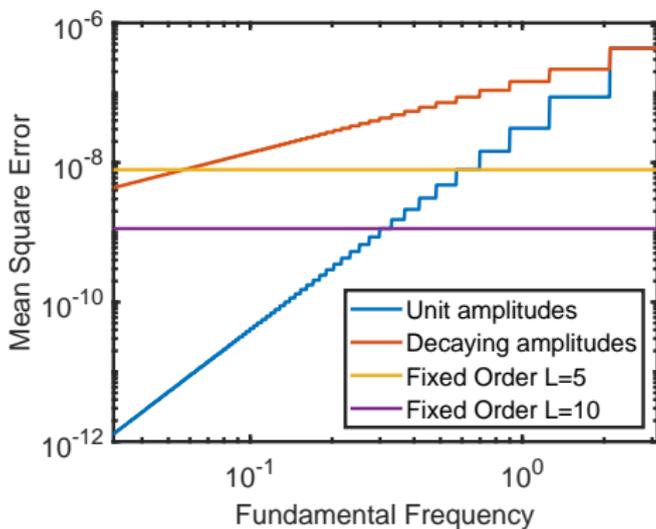


Figure: CRLB as a function of  $\omega_0$  for different cases.



# Fundamental Frequency Estimation

For white Gaussian noise ( $\mathbf{Q} = \sigma^2 \mathbf{I}$ ) with  $M = N$  the log-likelihood function is

$$\ln p(\mathbf{x}; \theta) = -N \ln \pi - N \ln \sigma^2 - \frac{1}{\sigma^2} \|\mathbf{x} - \mathbf{Z}\mathbf{a}\|_2^2. \quad (16)$$

The maximum likelihood estimator is given by (Quinn 1991)

$$\hat{\omega}_0 = \arg \max_{\omega_0} \ln p(\mathbf{x}; \theta) = \arg \max_{\omega_0} \mathbf{x}^H \mathbf{Z} (\mathbf{Z}^H \mathbf{Z})^{-1} \mathbf{Z}^H \mathbf{x} \quad (17)$$

$$\approx \arg \max_{\omega_0} \sum_{l=1}^L \left| \sum_{n=0}^{N-1} x(n) e^{-j\omega_0 l n} \right|^2. \quad (18)$$

This can be computed using an FFT, i.e., using *harmonic summation* (Noll 1969) but (17) can also be implemented fast (Nielsen 2017)!



# Fundamental Frequency Estimation

The principal angles  $\{\xi_k\}$  between the two subspaces with projection matrices  $\mathbf{\Pi}_Z$  and  $\mathbf{\Pi}_G$ , are defined for  $k = 1, \dots, K$  as (with  $K = \min\{2L, M - 2L\}$ )

$$\cos(\xi_k) = \max_{\mathbf{y}} \max_{\mathbf{z}} \frac{\mathbf{y}^H \mathbf{\Pi}_Z \mathbf{\Pi}_G \mathbf{z}}{\|\mathbf{y}\|_2 \|\mathbf{z}\|_2} \triangleq \mathbf{y}_k^H \mathbf{\Pi}_Z \mathbf{\Pi}_G \mathbf{z}_k = \kappa_k, \quad (19)$$

with  $\mathbf{y}^H \mathbf{y}_i = 0$  and  $\mathbf{z}^H \mathbf{z}_i = 0$  for  $i = 1, \dots, k - 1$ . The  $\kappa_k$ s are related to the Frobenius norm as  $\|\mathbf{\Pi}_Z \mathbf{\Pi}_G\|_F^2 = \sum_{k=1}^K \kappa_k^2$ . Thus, we can estimate  $\omega_0$  and  $L$  as (Christensen 2009)

$$(\hat{\omega}_0, L) = \arg \min_{\omega_0, L} \frac{1}{MK} \text{Tr} \left\{ \mathbf{Z} (\mathbf{Z}^H \mathbf{Z})^{-1} \mathbf{Z}^H \mathbf{G} \mathbf{G}^H \right\} \quad (20)$$

$$\approx \arg \min_{\omega_0, L} \frac{1}{MK} \|\mathbf{Z}^H \mathbf{G}\|_F^2. \quad (21)$$



# Fundamental Frequency Estimation

Recall that the filtered signal is  $y(n) = \mathbf{h}^H \mathbf{Z} \mathbf{D}(n) \mathbf{a} + \mathbf{h}^H \mathbf{e}$  and that

$$\mathbb{E} \{ |y(n)|^2 \} = \mathbf{h}^H \mathbf{Z} \mathbf{P} \mathbf{Z}^H \mathbf{h} + \mathbf{h}^H \mathbf{Q} \mathbf{h}. \quad (22)$$

Idea: design a filter as

$$\min_{\mathbf{h}} \mathbf{h}^H \mathbf{R} \mathbf{h} \quad \text{s.t.} \quad \mathbf{h}^H \mathbf{Z} = \mathbf{1}^T. \quad (23)$$

This has the solution

$$\mathbf{h}^* = \mathbf{R}^{-1} \mathbf{Z} (\mathbf{Z}^H \mathbf{R}^{-1} \mathbf{Z})^{-1} \mathbf{1}. \quad (24)$$

We can use this filter to estimate the fundamental frequency as (Christensen 2008)

$$\hat{\omega}_0 = \arg \max_{\omega_0} \mathbf{h}^H \mathbf{R} \mathbf{h} \quad (25)$$

$$= \arg \max_{\omega_0} \mathbf{1}^T (\mathbf{Z}^H \mathbf{R}^{-1} \mathbf{Z})^{-1} \mathbf{1}. \quad (26)$$



# Pre-Whitening

Many estimators assume that  $\mathbf{Q} = \sigma^2 \mathbf{I}$ . How do we deal with colored noise? Suppose that  $\mathbf{e}(n) \sim \mathcal{N}(0, \mathbf{Q})$ . We can transform  $\mathbf{x}(n)$  as

$$\mathbf{A}^H \mathbf{x}(n) = \mathbf{A}^H \mathbf{s}(n) + \mathbf{A}^H \mathbf{e}(n). \quad (27)$$

Let  $\mathbf{A}$  be the Cholesky factor of  $\mathbf{Q}^{-1}$ , then  $\mathbf{A}^H \mathbf{Q} \mathbf{A} = \mathbf{I}$  and the noise is now distributed as  $\mathbf{A}^H \mathbf{e}(n) \sim \mathcal{N}(0, \mathbf{I})$ . This can be implemented as a filter and is called pre-whitening.

The matrix  $\mathbf{Q}$  can be estimated in a number of ways:

- ▶ Noise trackers (Gerkmann 2012)
- ▶ Parametric NMF (Srinivasan 2007, Jensen 2018)
- ▶ Harmonic model (Nørholm 2016, Quinn 2021)



# Separation & Noise Reduction

How do we deal with interference and noise? Introducing sources  $x_k(n)$  indexed by  $k$ , we obtain (Christensen 2008)

$$x(n) = \sum_{k=1}^K x_k(n) = \sum_{k=1}^K \left( \sum_{l=1}^{L_k} a_{k,l} e^{j\omega_k l n} + e_k(n) \right) \quad (28)$$

$$= \underbrace{\sum_{l=1}^L a_l e^{j\omega_0 l n}}_{\text{target}} + \underbrace{e(n)}_{\text{interference+noise}} \quad (29)$$

$e(n)$  is no longer Gaussian! The filtered signal  $\mathbf{x}(n)$  is

$$\mathbf{h}^H \mathbf{x}(n) = \mathbf{h}^H \mathbf{Z} \mathbf{D}(n) \mathbf{a} + \mathbf{h}^H \mathbf{e}. \quad (30)$$

If  $\mathbf{h}^H \mathbf{Z} = \mathbf{1}^T$  then  $\mathbf{h}^H \mathbf{Z} \mathbf{D}(n) \mathbf{a} = \mathbf{1}^T \mathbf{D}(n) \mathbf{a} = \sum_{l=1}^L a_l e^{j\omega_0 l n}$ .



# Separation & Noise Reduction

The output power can be written as  $E\{|y(n)|^2\} = \mathbf{h}^H \mathbf{Z} \mathbf{P} \mathbf{Z}^H \mathbf{h} + \mathbf{h}^H \mathbf{Q} \mathbf{h}$ .  
Optimal filters can be derived by as:

$$\min_{\mathbf{h}} \mathbf{h}^H \mathbf{Q} \mathbf{h} \quad \text{s.t.} \quad \mathbf{h}^H \mathbf{Z} = \mathbf{1}. \quad (31)$$

The solution to this problem is:

$$\mathbf{h}^* = \mathbf{Q}^{-1} \mathbf{Z} (\mathbf{Z}^H \mathbf{Q}^{-1} \mathbf{Z})^{-1} \mathbf{1}. \quad (32)$$

These filters attenuate noise and interference optimally!

Simplifications (Christensen 2010):

1.  $\mathbf{Q} = \mathbf{R} \rightarrow \mathbf{h}^* = \mathbf{R}^{-1} \mathbf{Z} (\mathbf{Z}^H \mathbf{R}^{-1} \mathbf{Z})^{-1} \mathbf{1}$ .
2.  $\mathbf{Q} = \sigma^2 \mathbf{I} \rightarrow \mathbf{h}^* = \mathbf{Z} (\mathbf{Z}^H \mathbf{Z})^{-1} \mathbf{1}$ .
3.  $\lim_{M \rightarrow \infty} M \mathbf{Z} (\mathbf{Z}^H \mathbf{Z})^{-1} = \mathbf{Z} \rightarrow \mathbf{h}^* = \frac{1}{M} \mathbf{Z} \mathbf{1}$ .



# Non-Stationarity

Can we deal with a time-varying fundamental frequency? A more general signal model is the following:

$$x(n) = \sum_{l=1}^L A_l e^{j\theta_l(n)} + e(n), \quad (33)$$

where  $\theta_l(t) = \int_0^t l\omega_0(\tau) d\tau + \phi_l$  is the instantaneous phase and  $\omega_0(t)$  is the fundamental frequency. If  $\omega_0(t) \approx \omega_0 + \alpha_0 t$ , we get

$$\theta_l(t) = \frac{1}{2} \alpha_0 l t^2 + \omega_0 l t + \phi_l, \quad (34)$$

where  $\alpha_0$  is the fundamental chirp rate. The resulting model is called the *harmonic chirp model* (HCM)!  $\alpha_0$  and  $\omega_0$  can be estimated with NLS (Christensen 2014, Nørholm 2016).

Optimal filters can be designed for the HCM too (Nørholm 2016)!



# Non-Stationarity

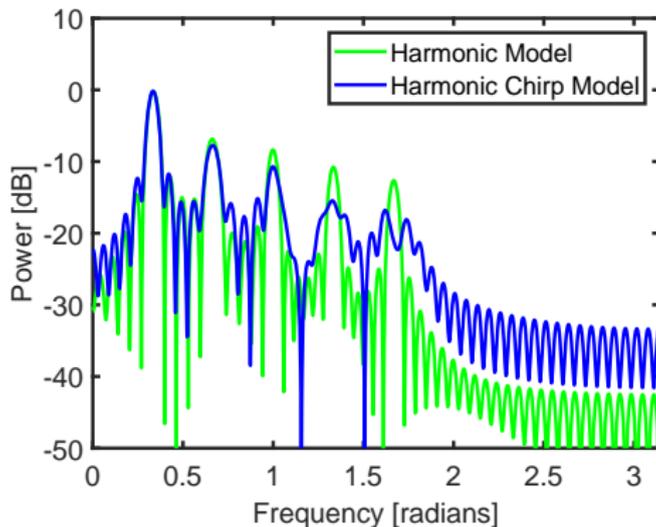
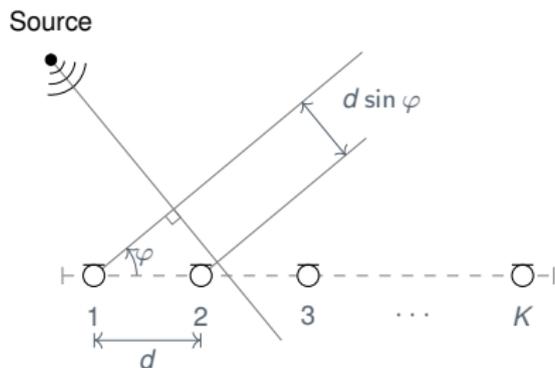


Figure: Spectrum of harmonic model and harmonic chirp model.



# Array Processing

Suppose we have a uniform linear array and sources in the farfield:



The delay between microphone 1 and  $k$  is then related to the angle  $\varphi$  as  $\Delta_k = \frac{d \sin \varphi}{c} f_s (k - 1)$  where  $f_s$  is the sampling frequency.



# Array Processing

Then we have that  $\mathbf{s}_k(n) = \mathbf{s}(n - \Delta_k)$  and  $\mathbf{x}_k(n) = \mathbf{s}_k(n) + \mathbf{e}_k(n)$  where  $k$  denotes the channel, and the signal for the  $k$ th channel is

$$\mathbf{x}_k(n) = \mathbf{ZD}(n - \Delta_k)\mathbf{a} + \mathbf{e}_k(n), \quad (35)$$

with  $\mathbf{e}_k$  being its noise. The signal at microphone  $k$  is then  $\mathbf{s}_k(n) = \mathbf{s}(n - \Delta_k)$  and thus (Jensen 2014)

$$\mathbf{s}_k(n) = \mathbf{ZD} \left( n - \frac{d \sin \varphi}{c} f_s(k - 1) \right) \mathbf{a}. \quad (36)$$

As we can see, it is easy to account for fractional delays and other geometries can easily be incorporated too.



# Array Processing

The observed signal can be organized in a matrix  $\mathbf{X}(n) \in \mathbb{C}^{K \times M}$  as

$$\mathbf{X}(n) = \begin{bmatrix} x_1(n) & \cdots & x_1(n - M + 1) \\ \vdots & \ddots & \vdots \\ x_K(n) & \cdots & x_K(n - M + 1) \end{bmatrix}. \quad (37)$$

Defining  $\mathbf{i}_k$  as the  $k$ th column of  $\mathbf{I}_K$ , the observed signal can be written as

$$\mathbf{X}^T(n)\mathbf{i}_k = \mathbf{ZD}(n - \Delta_k)\mathbf{a} + \mathbf{e}_k(n). \quad (38)$$

Define the spatial frequency  $\omega_s = \omega_0 f_s \frac{d \sin \varphi}{c}$  and the vectors

$$\mathbf{z}_t(\omega_0 l) = [1 \quad e^{-j\omega_0 l} \quad \cdots \quad e^{-j\omega_0 l(M-1)}]^T \quad (39)$$

$$\mathbf{z}_s(\omega_s l) = [1 \quad e^{-j\omega_s l} \quad \cdots \quad e^{-j\omega_s l(P-1)}]^T. \quad (40)$$



# Array Processing

By introducing  $\gamma_l(n) = a_l e^{j\omega_0 l n}$ , the matrix  $\mathbf{X}(n)$  can be modeled as

$$\mathbf{X}(n) = \sum_{l=1}^L \gamma_l(n) \mathbf{z}_s(\omega_s l) \mathbf{z}_t^T(\omega_0 l) + \mathbf{E}(n), \quad (41)$$

where  $\mathbf{E}(n) \in \mathbb{C}^{K \times M}$  is defined similarly to  $\mathbf{X}(n)$ . Defining  $\bar{\mathbf{x}}(n) = \text{vec}\{\mathbf{X}(n)\}$  where  $\text{vec}\{\cdot\}$  is the vectorization operator, the model can be written as

$$\bar{\mathbf{x}}(n) = \sum_{l=1}^L \gamma_l(n) \bar{\mathbf{z}}_l + \bar{\mathbf{w}}(n), \quad (42)$$

where  $\bar{\mathbf{z}}_l$  is the vectorized version of the spatio-temporal model, i.e.,

$$\bar{\mathbf{z}}_l = \text{vec}\{\mathbf{z}_s(\omega_s l) \mathbf{z}_t^T(\omega_0 l)\} \quad (43)$$

$$= \mathbf{z}_s(\omega_s l) \otimes \mathbf{z}_t(\omega_0 l). \quad (44)$$



# Array Processing

Defining the matrix  $\bar{\mathbf{Z}} = [\bar{\mathbf{z}}_1 \ \cdots \ \bar{\mathbf{z}}_L]$  we can impose the constraint  $\bar{\mathbf{h}}^H \bar{\mathbf{Z}} = \mathbf{1}^T$ , leading to the filter design problem:

$$\min_{\bar{\mathbf{h}}} \bar{\mathbf{h}}^H \bar{\mathbf{R}} \bar{\mathbf{h}} \quad \text{s.t.} \quad \bar{\mathbf{Z}}^H(n) \bar{\mathbf{h}} = \mathbf{1}, \quad (45)$$

where  $\bar{\mathbf{R}}$  is the covariance matrix of  $\bar{\mathbf{x}}(n)$ . The solution to the above optimization problem is given by:

$$\bar{\mathbf{h}}^* = \bar{\mathbf{R}}^{-1} \bar{\mathbf{Z}} (\mathbf{Z}^H \bar{\mathbf{R}}^{-1} \bar{\mathbf{Z}})^{-1} \mathbf{1}. \quad (46)$$

This yields the following estimator of  $\omega_0$  and  $\varphi$  (Jensen 2015):

$$\{\hat{\omega}_0, \hat{\varphi}\} = \arg \max_{\omega_0, \varphi} \mathbf{1}^T (\mathbf{Z}^H \bar{\mathbf{R}}^{-1} \bar{\mathbf{Z}})^T \mathbf{1}. \quad (47)$$

The filter can also be used for separation and noise reduction!



# Contributions

Key contributions of thesis:

- ▶ Methods for order estimation (Paper A)
- ▶ Optimal filters for periodic signals (Paper B, E)
- ▶ Fundamental frequency estimators (Paper C)
- ▶ Models, estimators, and filters for non-stationary signals (Paper D, E)
- ▶ Sparse linear prediction (Paper F)
- ▶ Model-based array processing (Paper G)



# Contributions

## Related contributions:

- ▶ The NLS fundamental frequency estimator can be implemented fast (Nielsen 2017) and in a Bayesian framework (Shi 2019)
- ▶ Subspace and optimal filtering methods can be unified (Jensen 2016)
- ▶ Model-based enhancement can improve speech intelligibility in babble noise (Kavelekalam 2019)
- ▶ Signal models can be used to detect string, fret, picking position, etc. (Hjerrild 2017)
- ▶ Parametric NMF can estimate statistics for pre-whitening (Nielsen 2018, Esquivel 2019)
- ▶ The model selection problem can be solved in a number of ways (Nielsen 2014)
- ▶ Real-time and stable sparse linear prediction possible (Jensen 2013, Giacobello 2014)



# Contributions

What can this all be used for?

- ▶ Hearing aids
- ▶ Voice analysis
- ▶ Telecommunication
- ▶ Reproduction systems
- ▶ Fault detection
- ▶ Music equipment

And many other things...



# Conclusions

- ▶ As we have seen, there are a number of advantages to the model-based approach.
- ▶ Critical assumptions can easily be identified and can be mitigated, if necessary.
- ▶ The harmonic model can be used for (approximately) periodic signals, such as speech and audio.
- ▶ It is possible to estimate its parameters in adverse conditions and computationally efficient implementations exist.
- ▶ It is possible to deal with noise, interference, and non-stationarity and to extend the principles to arrays.
- ▶ There are many more problems that could probably benefit from this approach!
- ▶ These include applications with multiple channels, adverse conditions, and when the fine details and the physics matter.

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# **AUDIO ANALYSIS LAB**

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